

Potential energy

Grade 11S – Physics

Unit Two: Mechanics

Energy in

Energy out

Chapter 11: Work & Energy

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Quiz 1:

Energy

20 min

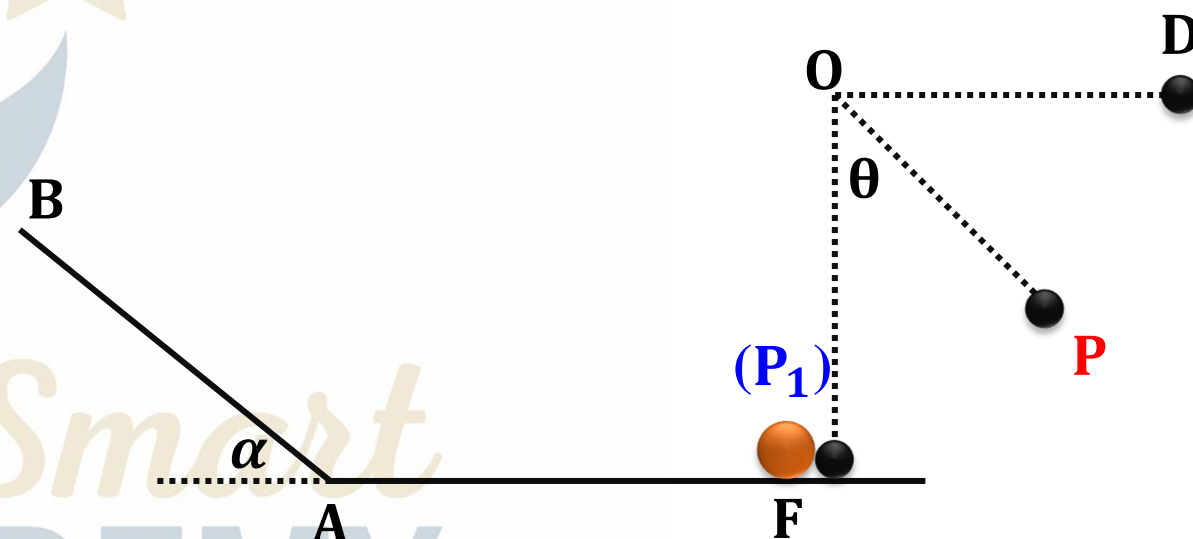


Consider pendulum is formed of an inextensible and mass less string of length $l = 0.45m$ having one of its ends fixed while the other end carries a particle (P) of mass $100g$. $g = 10m / s^2$.

The pendulum is shifted from its equilibrium position by $\theta_m = 90^\circ$, then released without initial velocity.

Take the horizontal plane containing FA as a gravitational potential energy reference for the system [(S), Earth].

We neglect friction on the axis through O and air resistance.



Quiz 1:

Energy

20 min



1. Calculate the initial mechanical energy of the system [(S),Earth] when (P) was at D.
2. Determine the expression of the mechanical energy of the system [(S),Earth] in terms of l, m, g, V and θ , where v is the speed of (P) when the string passes through a position making an angle θ with the vertical.
3. Determine the value of θ , ($0 < \theta < 90^\circ$), for which the kinetic energy of (P) is equal to the gravitational potential energy of the system [(S),Earth].
4. Calculate the magnitude of the velocity V_0 of (P) as it passes through its equilibrium position.

$l = 0.45\text{m}$; $m = 0.1\text{kg}$; $g = 10\text{m/s}^2$; $\theta_m = 90^\circ$, $V_D = 0\text{m/s}$; $f = 0\text{N}$

1. Calculate the initial mechanical energy of the system [(S),Earth] when (P) was at D.

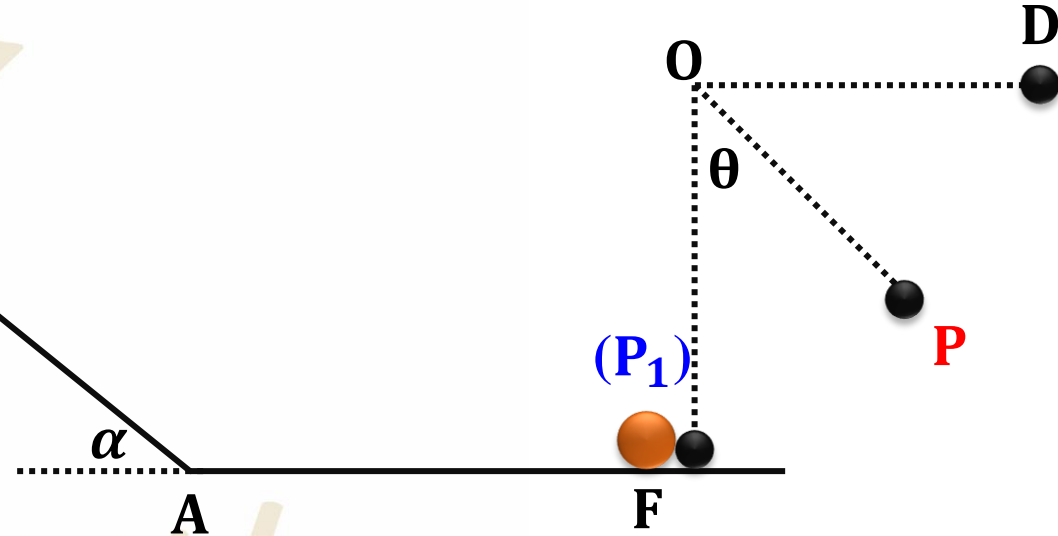
$$ME_D = KE_D + PE_D$$

$$ME_D = 1/2 m V_D^2 + mgh_D$$

$$ME_D = 1/2 (0.1)(0)^2 + 0.1 \times 10 \times l(1 - \cos\theta)$$

$$ME_D = 0 + 0.1 \times 10 \times 0.45(1 - \cos 90^\circ)$$

$$ME_D = 0.45\text{J}$$



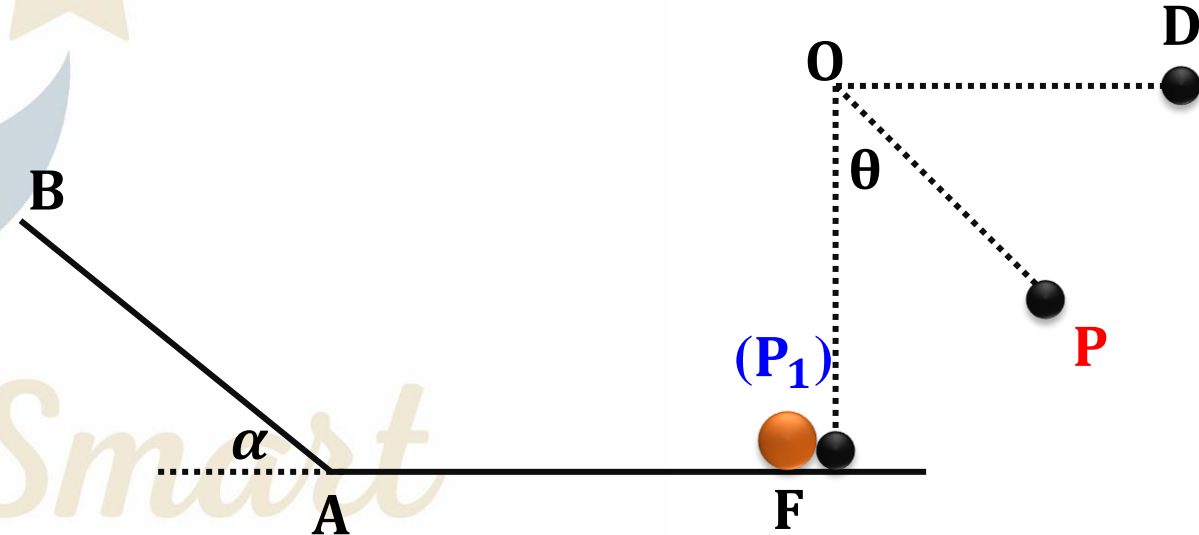
$$l = 0.45\text{m} ; m = 0.1\text{kg} ; g = 10\text{m/s}^2 ; \theta_m = 90^\circ, V_D = 0\text{m/s} ; f = 0\text{N}$$

2. Determine the expression of the ME of the system [(S),Earth] in terms of l, m, g, V and θ , where v is the speed of (P) when the string making an angle θ with the vertical.

$$ME = KE + PE$$

$$ME = \frac{1}{2}mV^2 + mgh$$

$$ME = \frac{1}{2}mV^2 + mgl(1 - \cos\theta)$$





$$l = 0.45\text{m} ; m = 0.1\text{kg} ; g = 10\text{m/s}^2 ; \theta_m = 90^\circ, V_D = 0\text{m/s} ; f = 0\text{N}$$

3. Determine the value of θ , ($0 < \theta < 90^\circ$), for which the kinetic energy of (P) is equal to the gravitational potential energy of the system [(S), Earth].

The ME is conserved, because friction is neglected; then:

$$ME = ME_D \Rightarrow KE + PE = 0.45\text{J}$$

But given $KE = PE$ then:

$$PE + PE = 0.45\text{J}$$

$$2PE = 0.45\text{J}$$

$$2mgl(1 - \cos\theta) = 0.45\text{J}$$

$$2 \times 0.1 \times 10 \times 0.45(1 - \cos\theta) = 0.45\text{J}$$

$$0.9(1 - \cos\theta) = 0.45\text{J}$$

$$1 - \cos\theta = \frac{0.45}{0.9}$$

$$1 - \cos\theta = 0.5$$

$$\cos\theta = 0.5 \Rightarrow \theta = 60^\circ$$

$$l = 0.45\text{m} ; m = 0.1\text{kg} ; g = 10\text{m/s}^2 ; \theta_m = 90^\circ, V_D = 0\text{m/s} ; f = 0\text{N}$$

4. Calculate the magnitude of the velocity V_0 of (P) as it passes through its equilibrium position

$$ME_0 = KE_0 + GPE_0$$

$$V_0^2 = \frac{0.45}{0.05}$$

$$0.45\text{J} = \frac{1}{2}mV_0^2 + mgh_0$$

$$V_0^2 = 9$$

$$0.45\text{J} = 0.5 \times 0.1V_0^2 + 0.1 \times 10(0)$$

$$V_0 = \sqrt{9}$$

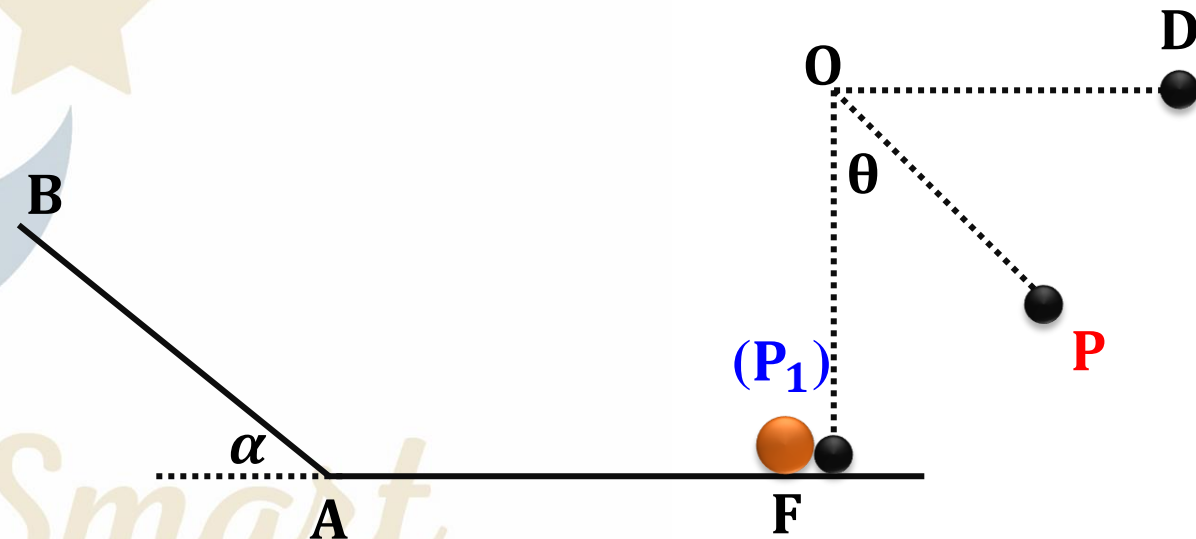
$$0.45\text{J} = 0.05V_0^2$$

$$V_0 = 3\text{m/s}$$

When (P) passes through the equilibrium position, the string is cut, and (P) enters in a collision with a stationary particle (P_1) of mass $m_1 = 200g$.

As a result of collision (P_1) moves along the frictionless horizontal track FA and reaches A with the speed $V_1 = 2m/s$.

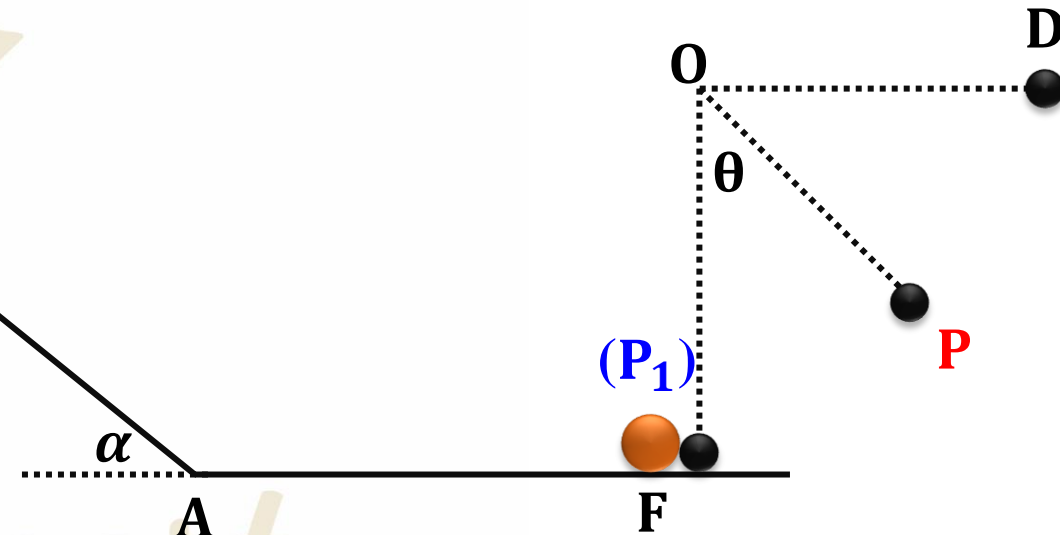
(P_1) continues along the line of greatest slope of the inclined plane AB that makes an angle $\alpha = 30^\circ$ with the horizontal.



a. Determine the altitude of the point M between A and B at which (P_1) turns back.

b. In fact, AB is not frictionless, (P_1) reaches a point N and turns back, where $AN = 20$ cm.

Calculate the magnitude of the force of friction (assumed constant) along AN.



$$m_1 = 0.2\text{kg}; g = 10\text{m/s}^2; f = 0\text{N}; V_1 = 2\text{m/s}; \alpha = 30^\circ$$

a) Determine the altitude of the point M between A and B at which (P₁) turns back.

At point M the particle (P₁) returns then: $V_M = 0$

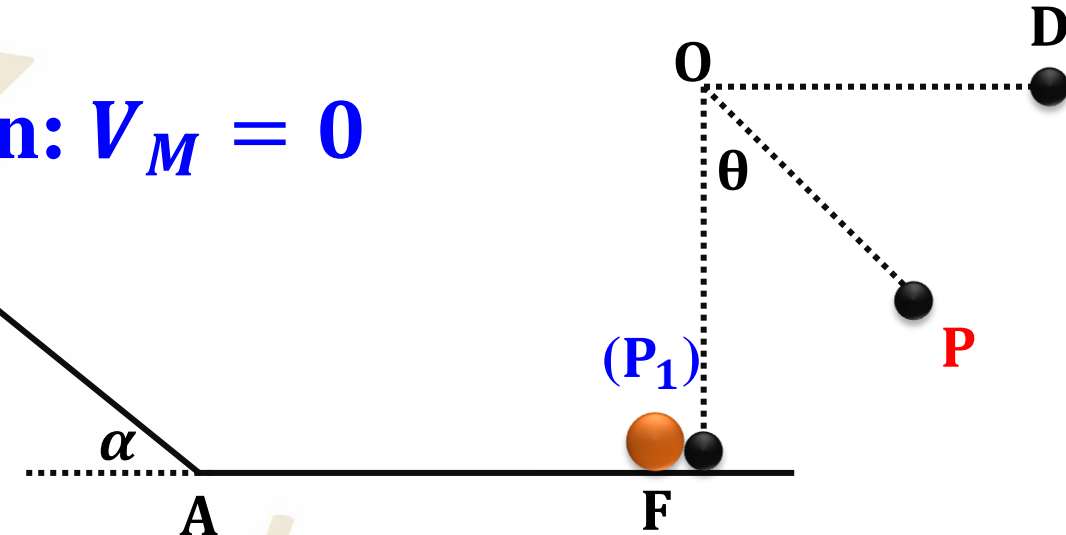
$$ME_A = ME_M$$

$$KE_A + PE_A = KE_M + PE_M$$

$$1/2 m_1 V_A^2 + m_1 g h_A = 1/2 V_M^2 + m_1 g h_M$$

$$0.5 \times 0.2 \times (2)^2 + 0 = 0 + 0.2 \times 10 \times h_M \quad \Rightarrow \quad 0.4 = 2 \times h_M$$

$$h_M = 0.2\text{m}$$



$$m_1 = 0.2\text{kg}; g = 10\text{m/s}^2; f = 0\text{N}; V_1 = 2\text{m/s}; \alpha = 30^\circ$$

b) In fact, AB is not frictionless, (P_1) reaches a point N and turns back, where $AN = 20\text{cm}$. Calculate the magnitude of the force of friction (assumed constant) along AN.

$$ME_N = KE_N + PE_N$$

$$ME_N = \frac{1}{2}m_1V_N^2 + m_1gh_N$$

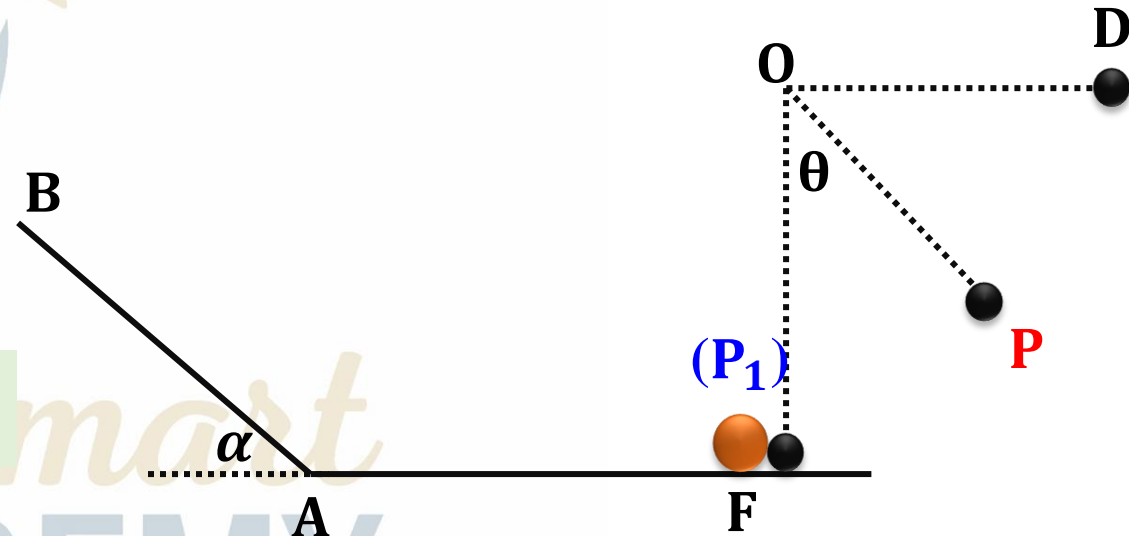
$$\sin\alpha = \frac{\text{opp}}{\text{hyp}} = \frac{h_N}{AN} \Rightarrow h_N = AN\sin\alpha$$

$$ME_N = 0 + mgAN\sin\alpha$$

$$ME_N = 0.2 \times 10 \times 0.2\sin 30$$



$$ME_N = 0.2\text{J}$$



$$\Delta ME_{A \rightarrow N} = W_{\vec{f_r}}$$

$$ME_N - ME_A = f \times d \times \cos(\alpha)$$

$$-0.2J = -f_r \times 0.2$$

$$ME_N - ME_A = f \times AN \times \cos(180)$$

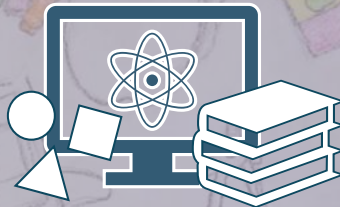
$$f_r = \frac{0.2}{0.2}$$

$$ME_N - ME_A = -f \times AN$$

$$0.2J - 0.4J = -f \times 0.2$$

$$f_r = 1N$$

The End





Quiz 2

Energy

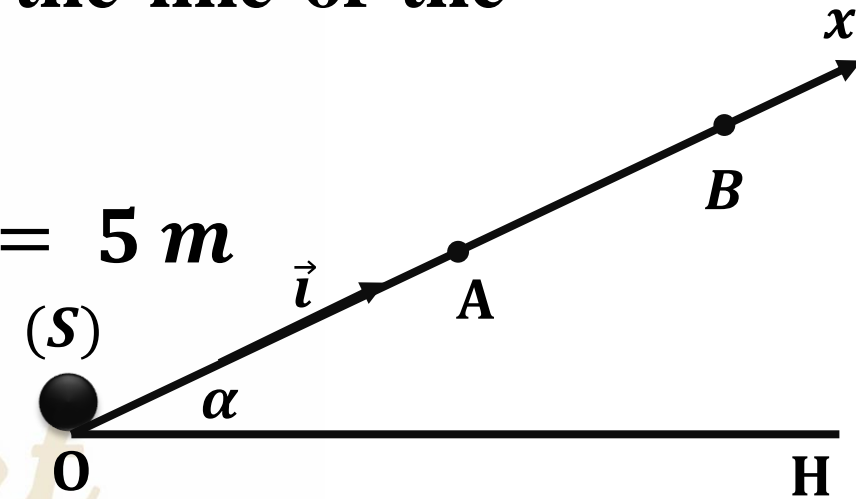
20 min



A particle (S), of mass $m = 500g$ is launched from the bottom O of the inclined plane that makes an angle $\alpha = 30^\circ$, at the instant $t_0 = 0$, with a velocity $\vec{V}_0 = V_0 \vec{i}$ along the line of the greatest slope (OB).

Let A be a point between O and B such that $OA = 5m$

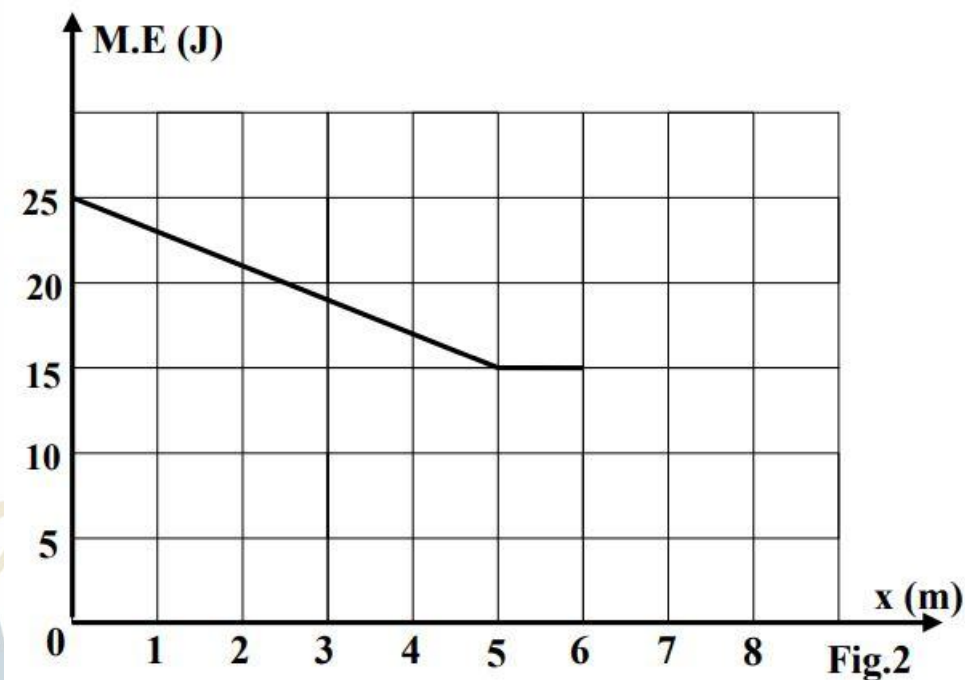
The position of (S), at the instant t , is given by x .



The horizontal plane passing through OH is a gravitational potential energy reference. Take: $g = 10m / s^2$.

The variation of the mechanical energy of the system [(S), Earth], as a function of x , is represented by the graph of (fig.2).

1. Determine using the graph the mechanical energy at point O then at point A.
2. Deduce the speed V_0 at O and the speed V at point A.
3. Show that (S) is subjected to a force of friction between the points O and A.



4. Calculate the variation of the mechanical energy of the system [(S), Earth] between O and A.

5. Deduce the magnitude of the force of friction, supposed constant, between O and A.

6. Determine, for $0 \leq x \leq 5$, the expression of the mechanical energy of the system [(S),Earth] as a function of x .

7. Determine the expression of mechanical energy between O and A using law of mechanical energy. Determine the speed of (S) at the point of abscissa $x = 6 \text{ m}$.

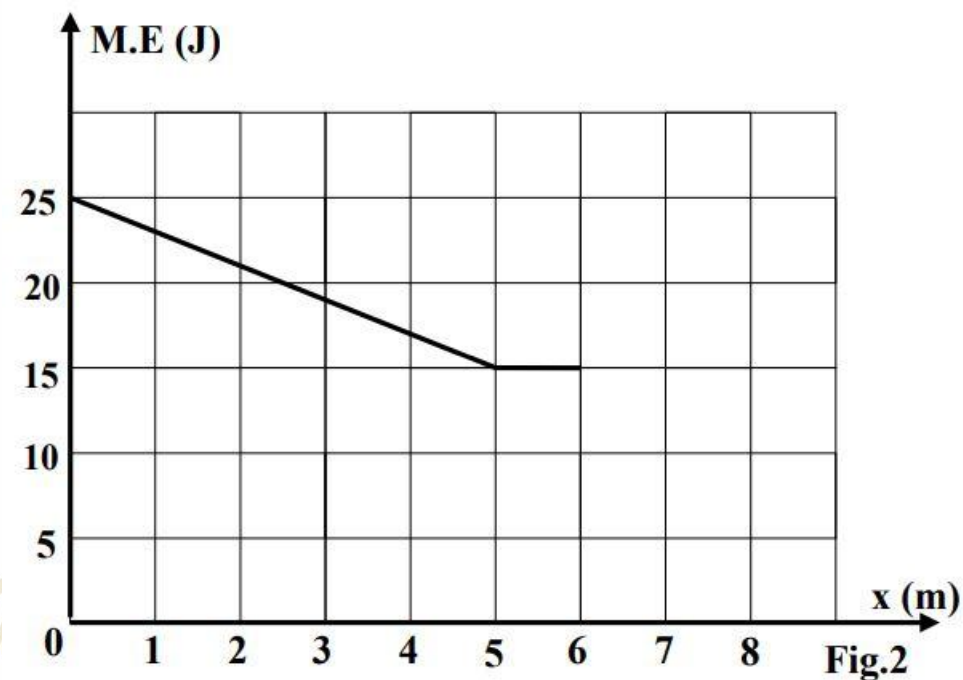


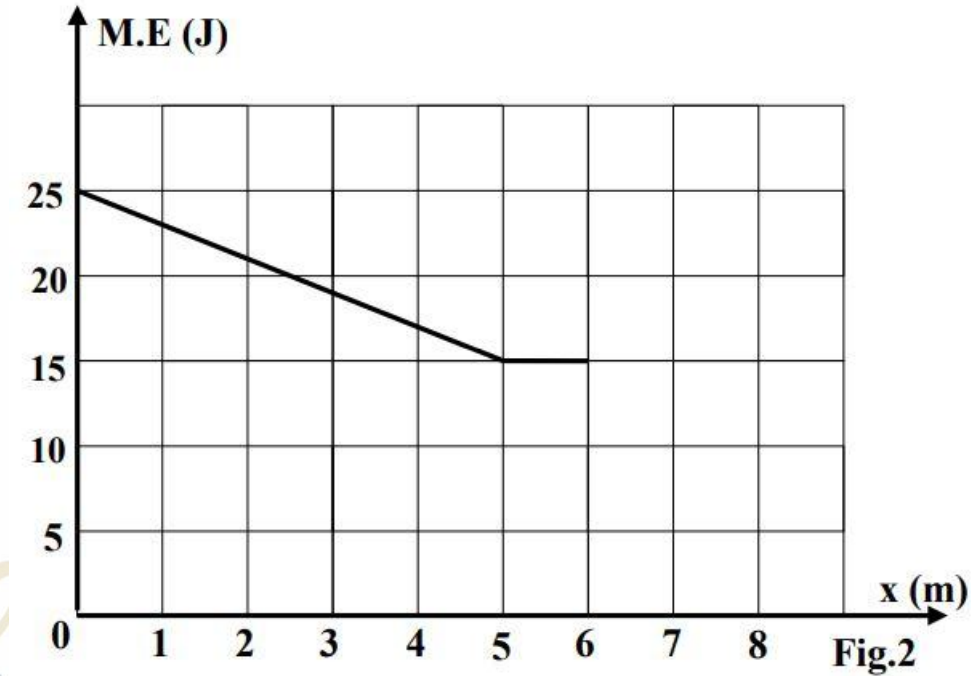
Fig.2

$$m = 0.5\text{kg}; \alpha = 30^\circ; OA = 5\text{ m}; g = 10\text{N/Kg}$$

1. Determine using the graph the mechanical energy at point O and A.

From the graph of figure 2:

- $ME_O = 25\text{J}$
- $ME_A = 15\text{J}$



$$m = 0.5\text{kg}; \alpha = 30^\circ; OA = 5\text{ m}; g = 10\text{N/Kg}$$

2. Deduce the speed V_0 at O and the speed V at point A.

$$ME_O = KE_O + PE_O$$

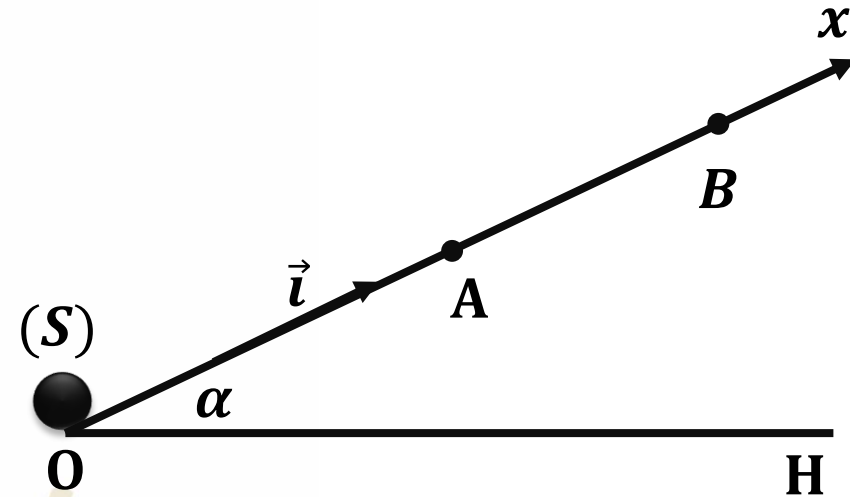
$$ME_O = \frac{1}{2} m V_0^2 + mgh$$

$$25\text{J} = \frac{1}{2} \times 0.5 \times V_0^2 + 0.5 \times 10(0)$$

$$25\text{J} = 0.25 \times V_0^2 \quad \Rightarrow \quad V_0^2 = \frac{25}{0.25} \quad \Rightarrow \quad V_0^2 = 100$$

$$V_0 = \sqrt{100}$$

$$V_0 = 10\text{m} / \text{s}$$



$$m = 0.5\text{kg}; \alpha = 30^\circ; OA = 5\text{ m}; g = 10\text{N/Kg}$$

$$ME_A = KE_A + PE_A$$

$$ME_A = 1/2 m V_A^2 + mgh_A$$

$$\sin\alpha = \frac{\text{opp}}{\text{hyp}} = \frac{h}{OA}$$

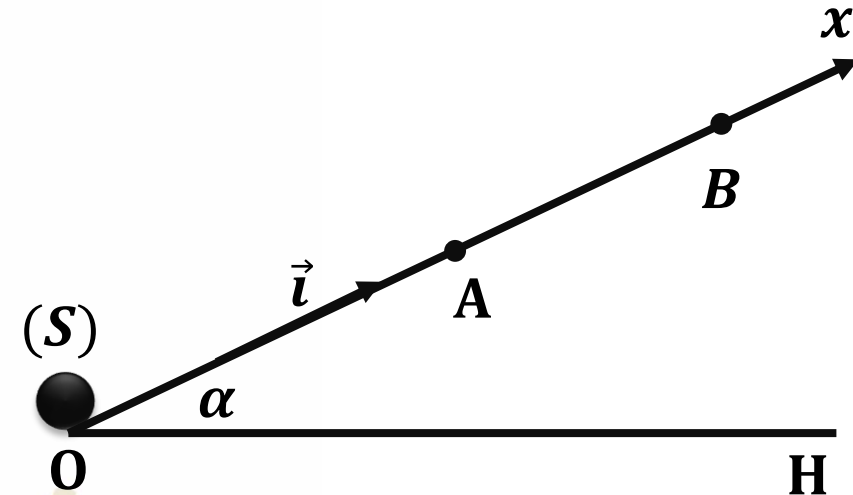
$$h = OA \sin\alpha$$

$$15\text{J} = 1/2 m V_A^2 + mgOA \sin\alpha$$

$$15\text{J} = 1/2 \times 0.5 \times V^2 + 0.5 \times 10 \times 5 \times \sin 30$$

$$25\text{J} = 0.25 V_A^2 + 12.5$$

$$V_A^2 = 50$$



$$12.5 = 0.25 V_A^2$$

$$V_A = V = 7.1\text{m} / \text{s}$$

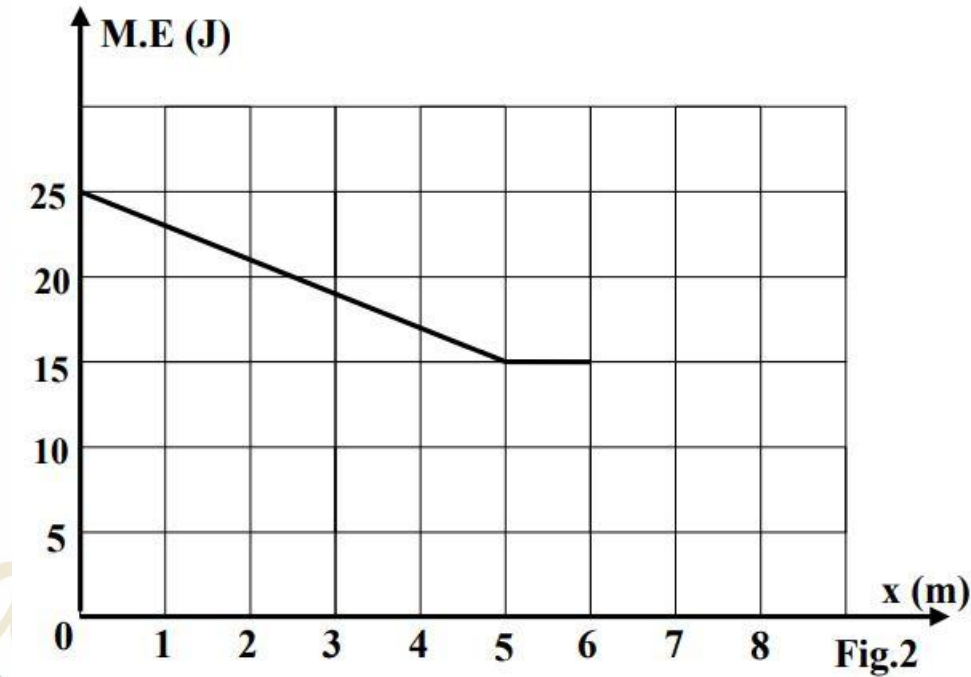
$$m = 0.5\text{kg}; \alpha = 30^\circ; OA = 5\text{ m}; g = 10\text{N/Kg}$$

3. Show that (S) is subjected to a force of friction between the points $x_0 = 0$ and $x_A = 5\text{m}$.

$$ME_O = 25\text{J} > ME_A = 15\text{J}$$

Then the solid (S) is subjected to a force of frictional.

4. Calculate the variation of the mechanical energy of the system [(S), Earth] between O and A.



$$\Delta ME_{O \rightarrow A} = ME_A - ME_O \quad \Rightarrow \quad \Delta ME_{O \rightarrow A} = 15\text{J} - 25\text{J}$$

$$\Delta ME_{O \rightarrow A} = -10\text{J}$$

$$m = 0.5\text{kg}; \alpha = 30^\circ; OA = 5\text{ m}; g = 10\text{N/Kg}$$

5. Deduce the magnitude of the force of friction, supposed constant, between O and A.

$$\Delta ME_{O \rightarrow A} = W_{\vec{f}}$$

$$\Delta ME_{O \rightarrow A} = f \times d \times \cos(\alpha)$$

$$\Delta ME_{O \rightarrow A} = f \times OA \times \cos(180)$$

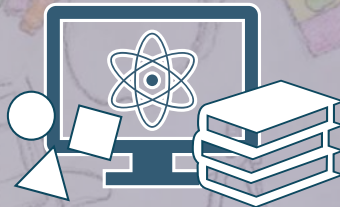
$$-10 = -f \times 5$$

$$f = \frac{10}{5}$$



$$f_r = 2\text{N}$$

The End





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